MODELLING OF NUCLEAR FUEL CLADDING TUBES CORROSION

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ABSTRACT. This paper describes materials made of zirconium-based alloys used for nuclear fuel cladding fabrication. It is focused on corrosion problems their theoretical description and modeling in nuclear engineering.

KEYWORDS: corrosion, zirconium alloys, nuclear fuel, cladding, modelling.

1. INTRODUCTION

Tubes covering nuclear fuel in current light water reactors (LWR) are made of zirconium-based alloys since the very origin of nuclear power utilization. Zirconium-based alloys were first used in nuclear reactors of U.S. nuclear submarines. Later, Zr was adopted by fuel vendors as a suitable material for fuel cladding for commercial reactors around the world. Zirconium has been chosen for its low cross section for neutron absorption, good corrosion resistance, and other outstanding thermomechanical characteristics.

Various degradation processes jeopardizing nuclear cladding integrity take place during reactor normal operation such as grid-to-rod fretting, debris-induced failures, crud-induced localized corrosion, waterside corrosion, and hydriding. This article is focused on water corrosion, its quantification, and theoretical description. Corrosion reaction caused mainly by an interaction of nuclear fuel cladding and coolant takes place on an external surface of cladding tubes, less frequently reacts internal cladding surface with oxygen released from pelets. In case of LWRs, metal reacts with water and zirconium oxide arises:

\[ \text{Zr} + 2\text{H}_2\text{O} \rightarrow \text{ZrO}_2 + 2\text{H}_2. \] (1)

Hydrogen released from the reaction described above partly dissolve in coolant water and partly penetrates tubes causing hydriding of zirconium. The fraction of hydrogen released from the reaction that is locally absorbed by the cladding tube is called pickup fraction and in PWR conditions is found to be constant for particular Zr-based alloys \textsuperscript{[4]}. Oxygen diffuses through the zirconium oxide layer and in an interface of metal and oxide causes additional oxidation. The density of the ZrO\textsubscript{2} is smaller than zirconium alloy density. The difference in density and different thermal expansion of materials is the primary cause of tension, internal stresses, and strains in cladding tubes. Moreover, thermal conductivity \( \lambda \) of ZrO\textsubscript{2} is much smaller than that of zirconium based alloys causing the Zirconium dioxide layer to decrease the heat transfer from the fuel pellet over the cladding to the coolant and consequently increase maximal temperature in the fuel pellet. The exact physical parameters depend on temperature and models of thermal conductivity of Zirconium dioxide. They are in details described in \textsuperscript{2} and \textsuperscript{3}. For example, the thermal conductivity of E110 alloy is about 18 W/mK at the temperature of 300°C. The thermal conductivity of the ZrO\textsubscript{2} for the same temperature is only about 2 W/mK.

Oxidation takes place also on the internal surface of fuel cladding, where metal reacts with oxygen released from the fuel pellets where fission takes place. When a high burn-up is reached, a bonding layer consisting of ZrO\textsubscript{2}, UO\textsubscript{2}, and fission products appears. This layer might be the cause of a firm connection between the fuel cladding and pellets.

2. ZIRCONIUM BASED ALLOYS

Zirconium-based alloys has been used as the nuclear fuel cladding since 1950s \textsuperscript{[6]}. There were originally two main groups of Zr-based alloys developed:

(1.) Zirconium-Tin and Iron-based alloys (originally developed in the U.S.)

(2.) Zirconium-Niobium based alloys (originally developed in former USSR)

During the evolution of the nuclear fuel, fuel vendors and research organizations developed dozens of concepts of fuel cladding alloys. However, the two main groups remained as can be seen in Figure \textsuperscript{1}.

Different cladding concepts can be based on the figure
3. Corrosion Models

The growth and development of the cladding corrosion layer for each zirconium-based alloy is usually expressed by corrosion models.

3.1. Garzarolli models

Models developed by Garzarolli et al. [8] are adopted for describing the thickness of the corrosion layer of cladding tubes made of Zircaloy-4, M5, and ZIRLO alloys under PWR conditions. These models generally based on Arrhenius law divide a growth of corrosion layer into two phases:

(1.) The first phase continues until a transition thickness of oxide layer $s_t$, is reached. The rate of corrosion layer growth is expressed by the cubic rate law – Equation (2) (original units and the temperature of oxide-metal interface is used) [2, 3].

\[
\frac{ds}{dt} = \frac{A}{s^2} \exp \left( -\frac{Q_1}{RT} \right),
\]

(2.) After reaching an alloy-specific transition thickness of oxide layer $s_{tr}$, second phase quantified by a linear differential Equation (3) taking into account also fast neutron flux $\Phi$ is adopted.

\[
\frac{ds}{dt} = (C_0 + U(M\Phi)^P) \exp \left( -\frac{Q_2}{RT} \right),
\]

where

- $s$ ... Oxide layer thickness [µm],
- $T$ ... Temperature [°C],
- $\Phi$ ... Neutron flux [neutrons/m²s],
- $A = 6.3 \times 10^6$ m³/day,
- $R = 1.98$ cal/molK,
- $C_0 = 8.04 \times 10^7$ µm/day,
- $M = 7.46 \times 10^{-15}$ cm²s/n,
- $P = 0.24$,
- $U = 2.59 \times 10^8$ µm/day.

Values of constants $Q_1$, $Q_2$ and transition thickness of oxide layer $s_{tr}$ are alloy-dependent and are summarized in Table 2 for four widely used alloys which were subject to many studies.

In literature, there were modifications of correlation models [2] and [3] defined. Modified models differ by values of constants and consider other physical phenomena neglected in the presented models. These models are implemented for example in FEMAXI and FRAPCON fuel performance codes.
### Table 1. Composition of zirconium-based alloys widely used around the world in PWRs as materials for cladding tubes fabrication [7].

<table>
<thead>
<tr>
<th>Alloying element</th>
<th>Zircaloy-4</th>
<th>ZIRLO</th>
<th>M5</th>
<th>E-110</th>
<th>E-635</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sn</td>
<td>1.2–1.7%</td>
<td>0.96–0.98%</td>
<td></td>
<td></td>
<td>1.25–1.30%</td>
</tr>
<tr>
<td>Fe</td>
<td>0.18–0.24%</td>
<td>0.094–0.105%</td>
<td>&lt;500 ppm</td>
<td>0.30–0.35%</td>
<td></td>
</tr>
<tr>
<td>Cr</td>
<td>0.07–0.13%</td>
<td>79–83 ppm</td>
<td>&lt;200 ppm</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Nb</td>
<td>1.02–1.04%</td>
<td>1.25–1.30%</td>
<td>0.8–1.2%</td>
<td>0.9–1.1%</td>
<td>1.0%</td>
</tr>
<tr>
<td>Al</td>
<td>36–38%</td>
<td>0.1%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ti</td>
<td>49–50%</td>
<td>0.2%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Zr</td>
<td>84–85%</td>
<td>1.07%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>O</td>
<td>900–1400 ppm</td>
<td>0.11–0.17%</td>
<td>&lt;1000 ppm</td>
<td></td>
<td>0.07%</td>
</tr>
<tr>
<td>N</td>
<td>&lt;65 ppm</td>
<td>22–30 ppm</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>C</td>
<td>150–400 ppm</td>
<td>60–80 ppm</td>
<td></td>
<td>&lt;200 ppm</td>
<td>&lt;200 ppm</td>
</tr>
</tbody>
</table>

### Table 2. Values of corrosion model’s constants used in corrosion models (2) and (3) as defined by [3].

<table>
<thead>
<tr>
<th></th>
<th>$Q_1$[cal/mol]</th>
<th>$Q_2$[cal/mol]</th>
<th>$s_{tr}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zircaloy-4</td>
<td>32289</td>
<td>27354</td>
<td>2 µm</td>
</tr>
<tr>
<td>M5</td>
<td>27446</td>
<td>29816</td>
<td>7 µm</td>
</tr>
<tr>
<td>ZIRLO</td>
<td>32289</td>
<td>27080</td>
<td>2 µm</td>
</tr>
<tr>
<td>Opt.ZIRLO</td>
<td>32289</td>
<td>27354</td>
<td>2 µm</td>
</tr>
</tbody>
</table>

### 3.2. THREE-PHASE MODEL

Another model for describing of Zircaloy-4 corrosion layer thickness in PWR conditions divides its evolution into three phases instead of two. The purpose is a faster oxide thickness growth after the second transition thickness is reached [7]. The model was developed by experimental data fitting and is more precise for higher values of oxide thickness than model developed by Garzarolli et al. [8]. Oxide layer growth during the first phase can be calculated by the following expression [6]

$$\frac{ds_3}{dt} = 2.187 \times 10^{-13} \exp \left( -\frac{135188}{RT} \right).$$  \hspace{1cm} (4)

The first transition thickness is the same as in the previous model – 2 µm for Zircaloy-4. Afterward, different formula is used instead of Equation [3]

$$\frac{ds}{dt} = \left( 9.31 \times 10^{-4} + 2.75 \times 10^{-3} \left( \frac{\Phi}{5.24 \times 10^{18}} \right)^{0.24} \right) \cdot \exp \left( -\frac{114526}{RT} \right).$$  \hspace{1cm} (5)

After reaching the second transition thickness – 35 µm, following equation is used

$$\frac{ds}{dt} = \left( 9.31 \times 10^{-4} + 2.75 \times 10^{-3} \left( \frac{\Phi}{5.24 \times 10^{18}} \right)^{0.24} \right) \cdot 1.8 \exp \left( -\frac{114526}{RT} \right).$$  \hspace{1cm} (6)

### 3.3. E110 CORROSION MODEL

A model describing the corrosion layer growth of E110 alloy in VVER conditions was developed by fitting experimental data at the Russian A.A. Bochvar High-technology Scientific Research Institute for Inorganic Materials. For the E110 alloy following relation was derived [9]

$$\frac{ds}{dt} = 40 \exp \left( -\frac{5147}{T} \right).$$  \hspace{1cm} (7)

Model was derived by data base on experiments, which took place in temperature range of 320–360°C. This model considers only one phase of corrosion layer development, transition thickness is disregarded. Comparison between corrosion layer growth of Zircaloy-4 and E110 is plotted in Figure 3.

The corrosion growth of E110 is considerably lower in comparison with the Zircaloy-4 alloy. Accelerating
growth can be seen for the Zircaloy-4 three-phase model which is not the case for the E110 alloy. For that reason, the neglecting of transitions in case of E110 is justified.

If the behavior of nuclear fuel during LOCA, RIA or other design basis accidents is calculated by fuel performance codes like FRAPTRAN or TRANSURANUS, the thickness of oxide layer is an initial condition which strongly influences a progress of the accident and its consequences.

4. CORROSION IN LOCA CONDITIONS

Large Break Loss of Coolant Accident (LBLOCA) is the maximal design basis accident of PWRs of second and third generation. During this accident, a temperature of the whole fuel rod including pellets quickly rises due to limited cooling conditions. The high temperature of fuel pellets leads to high-temperature gradients, stresses, and cracking of pellets. Rapid release of fission gases from the fuel can be observed and the internal pressure of filling gas rises.

The high temperature of cladding together with the high internal pressure can be a cause of a deformation, ballooning, or bursting of the cladding. This geometry changes can limit the coolant flow and further reduce the heat transfer from the fuel rods to the coolant.

Construction of reactor, design of the nuclear fuel and its properties must ensure that acceptance limits for LOCA accidents will not be violated:

1. A peak cladding temperature can nowhere exceed 1204 °C
2. Sufficient fuel rod strength upon quench taking into account an additional mechanical load (maintain post-quench ductility)
3. Fraction of zirconium reacted into oxide cannot exceed 1% (due to hydrogen production)
4. Melting temperature of fuel can not be reached in any place of the reactor core

4.1. CORROSION MODELS IN LOCA CONDITIONS

To develop corrosion models in LOCA conditions, it is necessary to measure experimental data in similar conditions. Experiments are done at high-temperature steam (800–1200 °C). Experiments with as-received cladding tubes and as well as with cladding tubes with corrosion layer has been performed. Preoxidation of experimental samples ensures that simulation will be performed in conditions which are similar to the real LOCA accident conditions with operating fuel.

A model of high-temperature corrosion of sponge based E110 alloy was developed at the UJP in the Czech Republic and is based on its experimental data [10]. Experiments cover a wide range of conditions (temperature 600–1300 °C and 0–480 minute long exposition). These wide conditions enable to use the model in various conditions and for various scenario for E110 alloy.

<table>
<thead>
<tr>
<th>No.</th>
<th>T [°C]</th>
<th>Process</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>600–750</td>
<td>Phases $\alpha + \beta$ transformation</td>
</tr>
<tr>
<td>2</td>
<td>750–950</td>
<td>Formation of $\beta$ phase</td>
</tr>
<tr>
<td>3</td>
<td>950–1100</td>
<td>Delated transformation, tetragonal oxide</td>
</tr>
<tr>
<td>4</td>
<td>1100–1300</td>
<td>Tetragonal oxide</td>
</tr>
</tbody>
</table>

Table 3. Physical processes taking place in zirconium E110 alloy in different temperature intervals during LOCA accident conditions.

This model describes a mass growth of oxide as defined in [10]

$$\Delta G = A \exp\left(\frac{E}{T}\right)t^n = kt^n,$$

where

$\Delta G$ … mass growth [mg/dm$^2$],
$A,E,k$ … fitting parameters,
$t$ … time [s],
$n$ … kinetic constant.

![Figure 4. Development of the parameter $n$ with temperature as defined by [10].](image)

For $n$ and $k$ parameters were derived following formulas

$$n = 0.4 \quad \text{for} \quad T < 768.4 \text{°C}$$

$$n = 2.609 - 4.898 \times 10^{-3}(T - 273.15) + 2.633 \times 10^{-9}(T - 273.15)^2$$

for $T < 960.3 \text{°C}$

$$n = 1.202 \times 10^{-3}(T - 273.15) - 0.8208$$

for $T < 1098.9 \text{°C}$

$$n = 0.5 \quad \text{for} \quad T > 1098.9 \text{°C}$$
Figure 6. Power history of rods BSM-25 and BK365.

Figure 7. Oxide layer thickness of BSM-25 and BK365 rods.

\[ k = 85265.6 \exp \left( -\frac{9875.59}{T} \right) \quad \text{for} \quad T < 934.1 \degree C \]  
\[ k = 1072.21 \exp \left( -\frac{4592.6}{T} \right) \quad \text{for} \quad T < 1054.5 \degree C \]  
\[ k = 33.33 \quad \text{for} \quad T < 1098.0 \degree C \]  
\[ k = 96482.3 \exp \left( -\frac{10913.1}{T} \right) \quad \text{for} \quad T > 1098.0 \degree C \]

Temperature intervals of equations (9)–(16) approximately correspond to physical processes, which take place in the cladding material during LOCA accident. These processes are described in Table 3.

This model well describes a corrosion kinetic for all ranges of temperature covered by experiment. The value of parameter \( n \) is 1/2 for high-temperature corrosion and 1/3 for middle-temperature corrosion. These values are the same as in other used models. Another model for \( n \) also very well describes the \( n \) temperature reliance.

Constant \( k \) equals approximately equals to 0 and increase with temperature to about 90 at 1300 \( ^\circ \)C. Dividing model into four ranges where different formulas are used brings a good agreement of the model with experimental data. A comparison between this model and data can be found in [10].

5. Model of Corrosion in FEMAXI

A calculation of oxide layer development in the FEMAXI-6 code has been performed for two fuel rods: BSM-25, and BK365. These rods were irradiated in the BR-3 reactor and reached burn-up of 66 and 52 MWd/kgHM. Rods were irradiated within the High Burnup Effect Program in the BR-3 reactor, cladding was made of Zircaloy-4 alloy, coolant inlet temperature was 255 \( ^\circ \)C.

A model originally developed by Garzarolli et al. [8] (Equations (2) and (3)) was used for the Zircaloy-4 alloy corrosion modeling. The two power histories used as a model input are plotted in Figure 6. Corresponding oxide layer thickness growth is shown in Figure 7. For both tested fuel rods, an average thickness and the maximal oxide layer thickness are shown. Maximal thickness of the corrosion layer is about two times higher than the average value. Maximal thickness was reached in the middle of the fuel rod which does
not correspond to the case in commercial power reactors. The oxide layer growth is strongly dependent on the temperature, the higher the temperature is the faster the growth. Therefore, the maximal thickness of the zirconium oxide layer in commercial power reactors is at the top of the fuel rod where the coolant temperature is highest.

Figure 7 shows that higher linear heat rate causes faster oxide layer creation. The graph also shows that the first phase of oxide layer growth is independent of fast neutron flux. Small differences are caused by higher temperature. In the later phase of fuel rod’s irradiation, there is a clear dependance of corrosion layer thickness on fast neutron flux and linear heat rate. When BSM-25 rod was operating in high heat rate condition, layer growth was much faster than in the case of smaller heat rate of the second fuel rod. Higher heat rate (and corresponding temperature) causes the bigger corrosion layer, even when the burnup of the BSM-25 rod is lower.

6. CONCLUSION
This article describes models quantifying corrosion of nuclear fuel cladding tubes made of zirconium-based alloys widely used in nuclear industry in nominal conditions and LOCA accident conditions. Models used for calculating of an oxide layer thickness in normal operation conditions for the widely used alloys Zircaloy-4, ZIRLO, M5 and E110 are presented and compared. A model for corrosion and high-temperature oxidation in LOCA conditions is described and reliance of particular parameters used in models are shown in graphs. A corrosion model for nominal conditions was applied in the FEMAXI-6 code to calculate corrosion of fuel rods BK363 and BSM-25 tested in the BR-3 reactor. The relations of burnup, linear heat rate, and corrosion layer thickness growth is illustrated in the example. Results show faster oxide growth in case of BSM-25 rod after reaching the transition thickness for Zircaloy-4 alloy, because this rod was operated at higher linear heat rate.

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REFERENCES