

# THE TIME DELAY OF AIR/OXYGEN MIXTURE DELIVERY AFTER THE CHANGE OF SET $FiO_2$ : AN IMPROVEMENT OF A NEONATAL MATHEMATICAL MODEL

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## Abstract

Oxygen therapy is an essential treatment of premature infants suffering from hypoxemia. Normoxemia is maintained by an adjustment of the fraction of oxygen ( $FiO_2$ ) in the inhaled gas mixture that is set manually or automatically based on peripheral oxygen saturation ( $SpO_2$ ). Automatic closed-loop systems could be more successful in controlling  $SpO_2$  than traditional manual approaches. Computer models of neonatal oxygen transport have been developed as a tool for design, validation, and comparison of the automatic control algorithms. The aim of this study was to investigate and implement the time delay of oxygen delivery after a change of set  $FiO_2$  during noninvasive ventilation support to enhance an available mathematical model of neonatal oxygen transport. The time delay of oxygen delivery after the change of  $FiO_2$  during the noninvasive nasal Continuous Positive Airway Pressure (nCPAP) ventilation support and during the High Flow High Humidity Nasal Cannula (HFHNC) ventilation support was experimentally measured using an electromechanical gas blender and a physical model of neonatal lungs. Results show the overall time delay of the change in the oxygen fraction can be divided into the baseline of delay, with a typical time delay 5.5 s for nCPAP and 6.5 s for HFHNC s, and an exponential rising phase with a time constant about 2–3 s. A delay subsystem was implemented into the mathematical model for a more realistic performance when simulating closed-loop control of oxygenation.

## Keywords

computer model, oxygen support, neonatal oxygen transport, respiratory system, time delay

## Introduction

Oxygen therapy is an essential treatment of premature infants suffering from hypoxemia due to the underdevelopment of the nervous, respiratory or cardiovascular system [1, 2]. Apart from the invasive mechanical ventilation, the inhaled gas mixture with an increased fraction of oxygen ( $FiO_2$ ) can be delivered by the noninvasive nasal Continuous Positive Airway Pressure (nCPAP) ventilation support or by the High Flow High Humidity Nasal Cannula (HFHNC) [3]. Hypoxemia leads to insufficient oxygenation of tissues, hypoxia, and consequent slow development of vital organs. The oxygen therapy, on the other hand, brings the risk of hyperoxemia, which can negatively impact especially the eye retina and the lungs [1]. Traditionally,  $FiO_2$  is adjusted manually based on peripheral oxygen saturation ( $SpO_2$ ) measured by pulse oximetry. Not only is the manual control of oxygenation time consuming, but several studies documented that clinical staff often fails

to keep  $SpO_2$  within the required range, sometimes even more than 50% of the time [4, 5]. On the contrary, automatic closed-loop systems that adjust  $FiO_2$  continuously could be more successful in controlling  $SpO_2$  and thus assuring required levels of oxygenation in premature infants [6–8].

Mathematical models of the  $FiO_2$ – $SpO_2$  relation in a premature infant are used during the development of the automatic control algorithms [7, 9–11]. Morozoff et al. presented a computer model that was implemented in the Matlab–Simulink programming environment (Mathworks, USA) and included four subsystems: air/oxygen blender, neonate, pulse oximeter, and controller [7, 9]. In the model, the time delay between the change of settings of the air/oxygen blender and an actual change of  $FiO_2$  in the airways was not included [7, 9, 10]. In an effort to enhance the available mathematical model of neonatal oxygen transport, the aim of this study was to investigate and implement the time delay of oxygen delivery after the change of set  $FiO_2$  during the noninvasive ventilation support.

## Laboratory experiment

A laboratory experiment was performed to measure the time delay of oxygen delivery into the airways after the set fraction of oxygen (sFiO<sub>2</sub>) was changed in a gas blender of a ventilator. The experiment was conducted in laboratories of the Faculty of Biomedical Engineering in Kladno under standard laboratory conditions. The experiment did not require any live subjects.

### Material and methods

The experiment consisted of measurements in two configurations: with the nCPAP ventilator MedinCNO (Medical Innovations GmbH, Germany) and with the HFHHNC ventilator Precision Flow Plus (VapoTherm Inc., USA). The ventilators were used as adjustable sources of the desired gas mixture due to their internal electromechanical gas blenders and digital user interface.

The setup of the experimental configuration with the nCPAP ventilator and the Medijet (Medical Innovations GmbH, Germany) nostril system is presented in Fig. 1. In the second experimental configuration, the HFHHNC ventilator with a system of nasal cannulas replaced the nCPAP ventilator and the nostril system. A small glass bottle was used as a physical model of the lungs due to the similarity of its mechanical properties—resistance and compliance—with the neonatal respiratory system. The volume of the glass bottle was 80 mL. The connecting tubes for the ventilators and the monitor of vital signs, used in the experiment, were original equipment supplied by manufacturers of the devices. The measured fraction of oxygen (mFiO<sub>2</sub>) in the physical model was measured by E-COVX module of a patient monitor Carescape Monitor B650 (GE Healthcare, Finland). The overall delay of the response of the oxygen analyzer module was 2.9 s and consisted of the sampling delay 2.5 s and the rise time delay 0.4 s as specified by the operator's manual. Data from the patient monitor were collected by the Datex-Ohmeda S/5 Collect software (GE Healthcare, Finland) and analyzed in Matlab R2018a (Mathworks, USA).

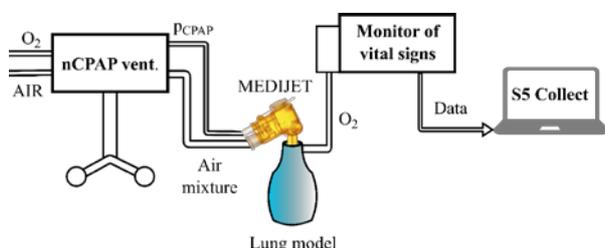


Fig. 1: The experimental setup with the nCPAP ventilator, nostril system, monitor of vital signs and physical model of the lungs for measurement of the time delay of oxygen delivery into the airways after the change of the set oxygen fraction.

At the beginning of a measurement, the ventilator was connected to the oxygen and air outlets and all devices were switched on. Initially, sFiO<sub>2</sub> was set to 21%. After mFiO<sub>2</sub> was stable, sFiO<sub>2</sub> was increased to 31% (the set fraction change: ΔsFiO<sub>2</sub> = +10%). The time of the step change command was referred to as the zero time. After a new steady state of mFiO<sub>2</sub> was reached, sFiO<sub>2</sub> was set back to the original value of 21% (ΔsFiO<sub>2</sub> = -10%). The same procedure with the step change of sFiO<sub>2</sub> from 21% to 51% (ΔsFiO<sub>2</sub> = +30%) and back to 21% (ΔsFiO<sub>2</sub> = -30%) followed. The measurements were repeated with the nCPAP and HFHHNC ventilators for various volumetric flow rates of the gas mixture in the ventilator circuit. The gas flow rates were 2–12 L/min with an increment of 2 L/min in case of the nCPAP system and 1–8 L/min with an increment of 1 L/min in case of the HFHHNC system.

The evaluated overall time delay of the change in the oxygen fraction was divided into two parts, Time 1 and Time 2, as shows an example in Fig. 2. Time 1 represents the baseline of delay, where mFiO<sub>2</sub> does not change, and it was measured from the zero time to the point where mFiO<sub>2</sub> started to rise. Measured Time 1 was reduced by 2.5 s of the sampling delay of E-COVX module. Time 1 was evaluated for each ΔsFiO<sub>2</sub> and gas flow rate.

The raising part of the mFiO<sub>2</sub> signal was fitted with a modified exponential function

$$y(t) = a(1 - e^{-t/\tau}) + b,$$

where  $t$  represents time (s). Values of the time constant  $\tau$  and the parameters  $a$  and  $b$  were found by a curve fitting algorithm (Curve Fitting Toolbox, Matlab) to provide the best fit of the function to the measured mFiO<sub>2</sub> waveform in the least-square sense. For each ΔsFiO<sub>2</sub>, the mean exponential curve was calculated as an average of exponential curves fitted to waveforms measured at individual gas flow rates. Time 2 that was used in consequent calculations was estimated as  $\tau$  of the mean exponential curve. Calculated Time 2 was reduced by 0.4 s of the rise time delay of E-COVX module.

Time 1 and Time 2 were processed separately for the nCPAP ventilator system and for the HFHHNC ventilator system. The overall time delay of oxygen delivery after the change in the set oxygen fraction is the sum of Time 1 for the respective gas flow rate and ΔsFiO<sub>2</sub> and of Time 2 for the respective ΔsFiO<sub>2</sub>.

### Results

Table 1 summarizes Time 1 that represents the baseline of delay of the mFiO<sub>2</sub> signal for various step changes of sFiO<sub>2</sub> and various levels of gas flow rate. The sampling delay of the patient monitor was subtracted from the data before they were reported in the table. Median Time 1 was 5.5 s (IQR 4.5–7.5) for nCPAP and 6.5 s (IQR 2.5–8.5) for HFHHNC.

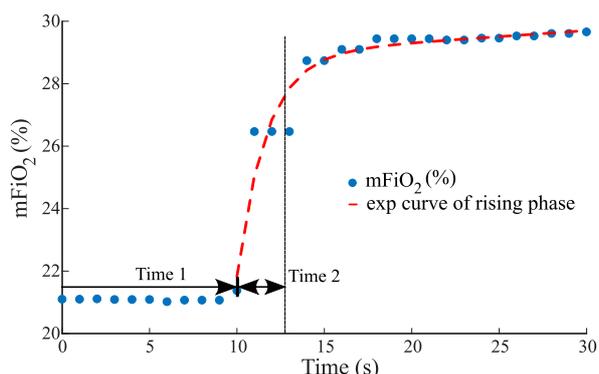


Fig. 2: The overall delay of  $mFiO_2$  with the baseline of delay (Time 1) and the rising phase (Time 2) after  $sFiO_2$  increased from 21% to 31%. In the rising phase, the  $mFiO_2$  data were fitted with the exponential function for estimation of the time constant. The gas flow rate was 6 L/min.

Table 2 reports parameters of the mean exponential curves calculated from the raising part of the  $mFiO_2$  signal for each  $\Delta sFiO_2$ , including the time constant  $\tau$  used as an estimate of Time 2. The quality of the fit of the mean exponential curve to all the  $mFiO_2$  data related to the same  $\Delta sFiO_2$  was estimated by the coefficient of determination  $R^2$ . In all fits  $R^2$  was higher than 0.90 which indicates a good agreement between the model and the data. Generally,  $\tau$  is similar for the positive and for the negative  $\Delta sFiO_2$  in the case of the nCPAP system and for the positive  $\Delta sFiO_2$  in the case of HFHHNC. An estimated  $\tau$  for negative  $\Delta sFiO_2$  in the case of HFHHNC is smaller. The range of parameters  $a$  and  $\tau$  is considerably wider for HFHHNC data than for nCPAP data.

### Implementation of the delay subsystem in the computer model

Based on the measured time delay of oxygen delivery into the airways, a delay subsystem was implemented in Simulink and integrated into the mathematical model of neonatal oxygen transport. A principal scheme of the delay subsystem is presented in Fig. 3.

The inputs to the delay subsystem are the current values of  $sFiO_2$  and gas flow rate in the model gas blender. The output of the delay subsystem is the current  $FiO_2$  of the inhaled gas mixture. The delay subsystem compares input  $sFiO_2$  in every step of the simulation with its previous value and, if a change in  $sFiO_2$  is detected, it calculates the length of the delay. The delay subsystem combines the baseline of delay (based on Time 1) and the rising delay (based on Time 2) of the  $FiO_2$  signal. We utilized the values of Time 1 and Time 2 that were calculated for the nCPAP ventilator.

Table 1: The baseline of delay (Time 1) evaluated for various gas flow rates and step changes of the set fraction of oxygen in the nCPAP and HFHHNC ventilators.

nCPAP		Time 1 (s)			
Flow (L/min)	$\Delta sFiO_2$ +10%	$\Delta sFiO_2$ +30%	$\Delta sFiO_2$ -10%	$\Delta sFiO_2$ -30%	
2	16.5	10.5	8.5	8.5	
4	10.5	7.5	6.5	4.5	
6	7.5	4.5	5.5	3.5	
8	7.5	5.5	4.5	4.5	
10	5.5	4.5	4.5	3.5	
12	5.5	4.5	3.5	1.5	

HFHHNC		Time 1 (s)			
Flow (L/min)	$\Delta sFiO_2$ +10%	$\Delta sFiO_2$ +30%	$\Delta sFiO_2$ -10%	$\Delta sFiO_2$ -30%	
1	41.5	15.5	6.5	5.5	
2	19.5	8.5	4.5	3.5	
3	14.5	7.5	2.5	2.5	
4	10.5	8.5	3.5	2.5	
5	8.5	7.5	1.5	2.5	
6	6.5	5.5	1.5	1.5	
7	8.5	8.5	1.5	1.5	
8	7.5	7.5	2.5	2.5	

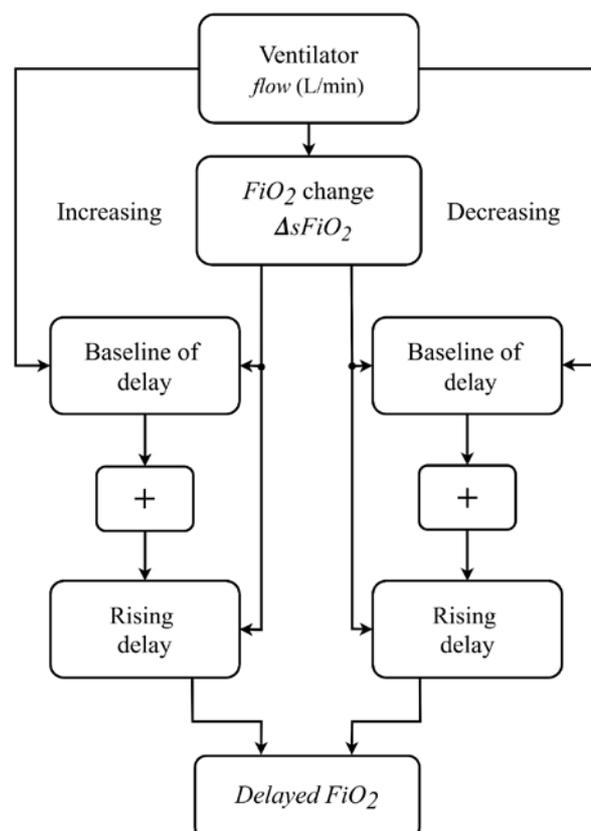


Fig. 3: A principal scheme of the delay subsystem used in the mathematical model of neonatal oxygen transport.

Table 2: Parameters of the mean exponential curves calculated from the raising part of the  $m\text{FiO}_2$  signal for each  $\Delta s\text{FiO}_2$  in the nCPAP and HFHHNC ventilators. Ranges of parameter values of individual exponential curves are presented in parentheses. The rise time delay of the patient monitor was subtracted from the  $\tau$  data before they were reported in the table. Note that  $\tau = \text{Time 2 (s)}$ .

nCPAP Parameter	Set fraction change			
	$\Delta s\text{FiO}_2$ +10%	$\Delta s\text{FiO}_2$ +30%	$\Delta s\text{FiO}_2$ -10%	$\Delta s\text{FiO}_2$ -30%
$a$	8.4 (8.2, 8.4)	24.2 (23.0, 26.1)	-8.3 (-8.2, -8.4)	-25.9 (-24.2, -27.2)
$b$	21.1 (20.9, 21.3)	22.4 (20.8, 24.0)	29.7 (29.6, 29.9)	48.1 (46.8, 48.9)
$\tau$	2.4 (1.7, 2.8)	2.7 (2.6, 3.9)	2.2 (1.6, 2.3)	2.9 (2.0, 3.5)
$R^2$	0.99	0.99	0.99	0.98

HFHHNC Parameter	Set fraction change			
	$\Delta s\text{FiO}_2$ +10%	$\Delta s\text{FiO}_2$ +30%	$\Delta s\text{FiO}_2$ -10%	$\Delta s\text{FiO}_2$ -30%
$a$	9.6 (9.0, 15.0)	30.2 (27.8, 32.4)	-9.1 (-8.8, -11.2)	-26.3 (-25.5, -32.3)
$b$	20.8 (19.2, 20.9)	19.2 (18.6, 21.0)	30.0 (29.3, 31.6)	48.7 (45.4, 52.1)
$\tau$	2.5 (0.5, 6.8)	2.2 (0.7, 2.3)	0.8 (0.0, 2.7)	1.4 (0.2, 2.4)
$R^2$	0.97	0.91	0.98	0.99

The baseline of delay is implemented using a time delay block available in Simulink. Six third-order polynomial functions were constructed that express the time delay as a function of gas flow rate and approximates the measured values of Time 1 in Table 1. For simulated  $\Delta s\text{FiO}_2 < 15\%$ , the polynomial function applies that is constructed from values measured for  $\Delta s\text{FiO}_2 = 10\%$ . For simulated  $\Delta s\text{FiO}_2 > 25\%$ , the polynomial function applies that is constructed from values measured for  $\Delta s\text{FiO}_2 = 30\%$ . For simulated  $15\% \leq \Delta s\text{FiO}_2 \leq 25\%$ , the respective polynomial function was constructed from averaged values measured for  $\Delta s\text{FiO}_2 = 10\%$  and  $\Delta s\text{FiO}_2 = 30\%$ . An analogous procedure applies for negative values of  $\Delta s\text{FiO}_2$ . Outliers were excluded from the approximations. The polynomial functions used for  $15\% \leq \Delta s\text{FiO}_2 \leq 25\%$  and  $-25\% \leq \Delta s\text{FiO}_2 \leq -15\%$  are shown in Fig. 4.

The rising delay is implemented using a dynamic rate limiter block that simplifies the exponential growth or decrease in  $\text{FiO}_2$  by a linear trend with its slope set as the magnitude of the simulated  $\Delta s\text{FiO}_2$  divided by the time constant derived as an average of measured values that were presented in Table 2. In other words, the overall simulated rising delay equals the time constant. The differences among measured values of the time constant in Table 2 are smaller than the used sampling rate of 1 Hz, which allows averaging. The averaged time constant value is 2.5 s for the positive  $\Delta s\text{FiO}_2$  and 2.6 s

for the negative  $\Delta s\text{FiO}_2$ . Thus, the rising delay approximates the upper boundary of the measured rate of change of  $\text{FiO}_2$  and—as implemented—it does not depend on the current gas flow rate. The chosen approach is illustrated in Fig. 2, which shows the major part of the  $\text{FiO}_2$  increase within Time 2, i.e. the time constant.

An example of the function of the  $\text{FiO}_2$  delay subsystem is given in Fig. 5 which compares the set  $\text{FiO}_2$  and delayed  $\text{FiO}_2$  in the computer simulation.

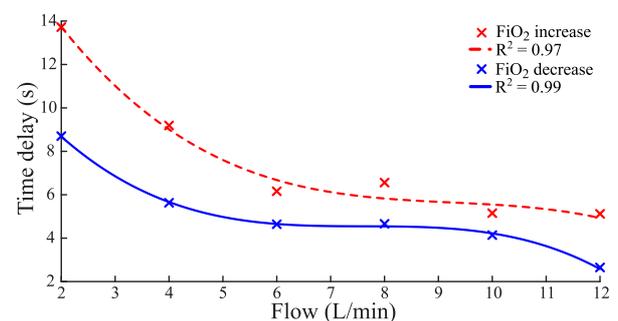


Fig. 4: Polynomial functions of the time delay for  $15\% \leq \Delta s\text{FiO}_2 \leq 25\%$  ( $\text{FiO}_2$  increase, red) and  $-25\% \leq \Delta s\text{FiO}_2 \leq -15\%$  ( $\text{FiO}_2$  decrease, blue) derived by averaging the data for the nCPAP ventilator in Table 2. The quality of the fit was estimated by the coefficient of determination  $R^2$ .

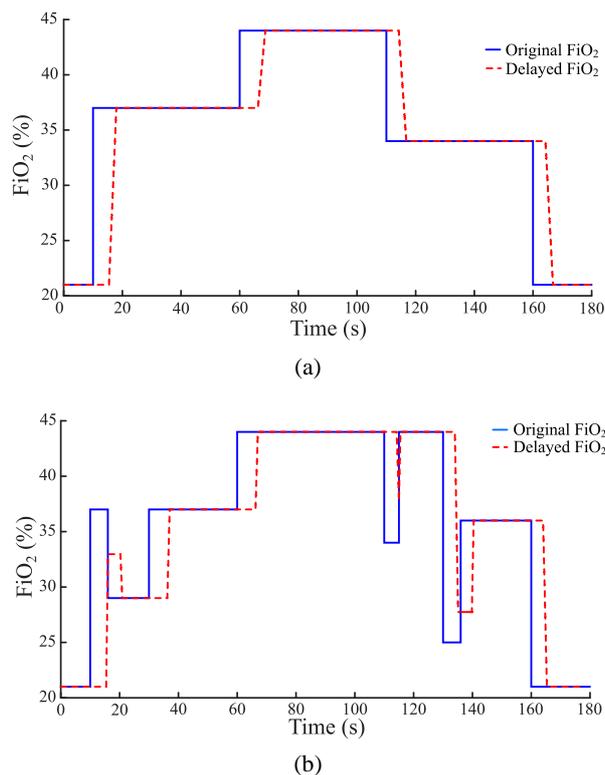


Fig. 5: Comparison of the set and the delayed  $\text{FiO}_2$  signal (i.e., the input and the output of the delay subsystem). The gas flow rate was 10 L/min. (a) The  $\text{FiO}_2$  increase was set at 10 s and 60 s and the  $\text{FiO}_2$  decrease was set at 110 s and 160 s after the start of the simulation. (b) Quick changes of set  $\text{FiO}_2$  were added in 10 s, 110 s and 130 s to demonstrate the effect of time delay in  $\text{O}_2$  delivery.

## Discussion

In this work we focused on the time delay of oxygen delivery after the change of set  $\text{FiO}_2$  in respiratory support systems with internal electronic gas blenders. Our laboratory experiment showed that the time delay should not be neglected in the developed mathematical model of neonatal oxygen transport as it is comparable with the time constants of the physiological processes simulated by the model. This is especially important when the model is used for testing of a closed-loop configuration where the oxygen fraction is automatically adjusted according to how the current  $\text{SpO}_2$  agrees with the desired  $\text{SpO}_2$  range.

In Table 1 we can see that with an increased gas flow rate the time delay decreases. Also, at lower gas flow rates the  $\text{FiO}_2$  increase takes longer time than the  $\text{FiO}_2$  decrease. At high flow rates, the time delay is similar for both the  $\text{FiO}_2$  increase and decrease. Table 2 shows  $\tau$  smaller for negative  $\Delta\text{FiO}_2$  in the case of HFHHNC when compared to the positive and the negative  $\Delta\text{FiO}_2$  in case of the nCPAP ventilation support and to the

positive  $\Delta\text{FiO}_2$  in case of HFHHNC. An actual difference was perhaps overemphasized due to the combination of a low sampling rate (1 Hz) and the subtraction of the measurement delay (0.4 s). Wider ranges of  $a$  and  $\tau$  in the case of HFHHNC measurements suggests lower accuracy of HFHHNC settings during the experiment and less reliable data. Nevertheless, it still seems that the HFHHNC system reacts a little faster to the decrease of  $\text{FiO}_2$  than the nCPAP system. That should be considered when designing precise simulation models or control systems.

The time delay we measured can be compared with patient data published by Fathabadi et al. [12] and in Krone's master thesis [11]. Fathabadi et al. reported the median of the time delay 22 s (IQR 8–40 s) during the  $\text{FiO}_2$  increase and 34 s (IQR 17–67 s) during the  $\text{FiO}_2$  decrease for various gas flow rates and variable magnitude of  $\text{FiO}_2$  change. Krone reported the time delay for the rising phase 25–105 s. In our mathematical model a simulation run in the nCPAP mode with the gas flow rate 5 L/min showed the overall delay 19.5 s of a  $\text{FiO}_2$  increase from 28% to 32%. However, Fathabadi's and Krone's delays include the delay of oxygen distribution to the lungs and the physiological delay of oxygen transport in the blood. Our measurement involves only the time delay in the mechanical part of oxygen delivery systems and does not include the variability of a neonatal organism.

The time delay presented in Table 1 and demonstrated in Figure 4 shows irregularities in the decreasing trend. The result could reflect a limited sensitivity of the oxygen sensor in low gas flow rates. Another limitation of the experiment is the sampling frequency 1 Hz of the Datex Ohmeda S/5 Collect software, which causes sharp step changes in the recorded  $\text{mFiO}_2$  signal.

The implementation of the delay subsystem in the mathematical model is based on the measurements taken for the nCPAP system. The time delay is divided into the baseline of delay and the rising phase. The rising phase is simplified based on the finding that after the baseline of delay the major changes in the actual  $\text{FiO}_2$  level occurred within the interval of 2–3 s, regardless of the magnitude of the change.

## Conclusion

In this work we presented the laboratory experiment to measure the time delay of oxygen delivery after the change of set  $\text{FiO}_2$  during the nCPAP or HFHHNC respiratory support. The experimentally measured data allowed an improvement of the mathematical model of neonatal oxygen transport by implementing the delay subsystem. Our enhancement of the existing model should increase its accuracy and usability as a tool for testing different approaches to oxygenation control of premature neonates.

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